

# Concepts for efficient production, transport and cooling of intense muon beams

Diktys Stratakis

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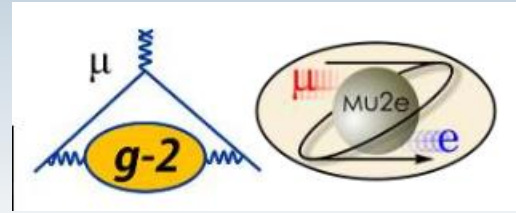
Accelerator Physics and Technology Seminar, Fermilab, Batavia, IL, USA

July 28, 2015

# Why muons?

- Carry the same electrical charge as electrons
- Like electrons, muons are elementary particles and thus can produce “clean collisions”
- Muons are 207 times heavier than electrons making it more sensitive to the discovery of new physics
- Unlike electrons, they can be accelerated and stored in circular rings at very high ( $\sim$ TeV) energies by taking advantage of their larger mass

# Current activity: Muon campus @ Fermilab



- **Mu2e:** The Mu2e experiment attempts to detect charged lepton flavor violation
- **g-2:** Precision measurement of magnetic properties of muons

<http://muon.fnal.gov/>

# Far future (?): Towards a Muon Collider

- Some benefits...
  - Large muon mass suppresses synchrotron radiation
  - Muons can be accelerated and stored using rings at much higher energy than electrons
  - As with an  $e^+e^-$  collider, a  $\mu^+\mu^-$  collider would offer a precision probe of fundamental interactions

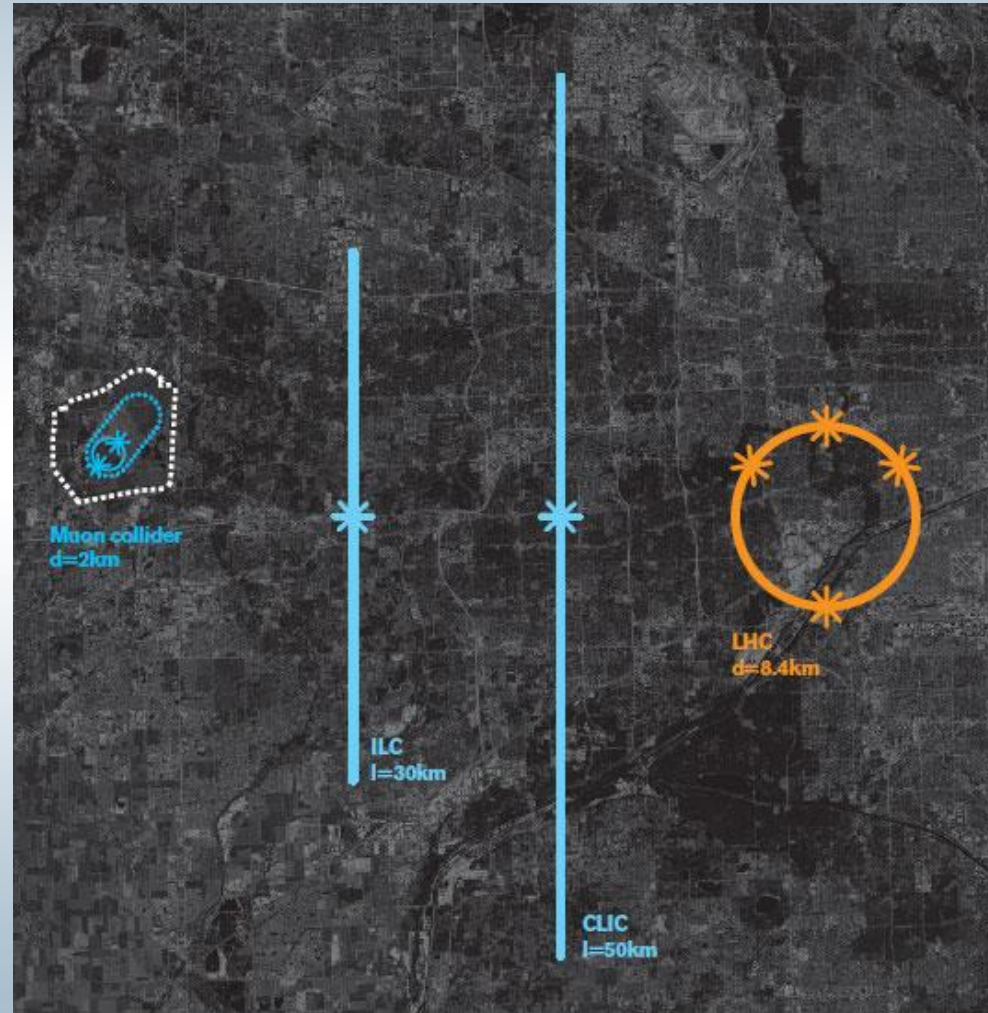


Image: [www.map.fnal.gov](http://www.map.fnal.gov)



# Muon Collider (MC) components

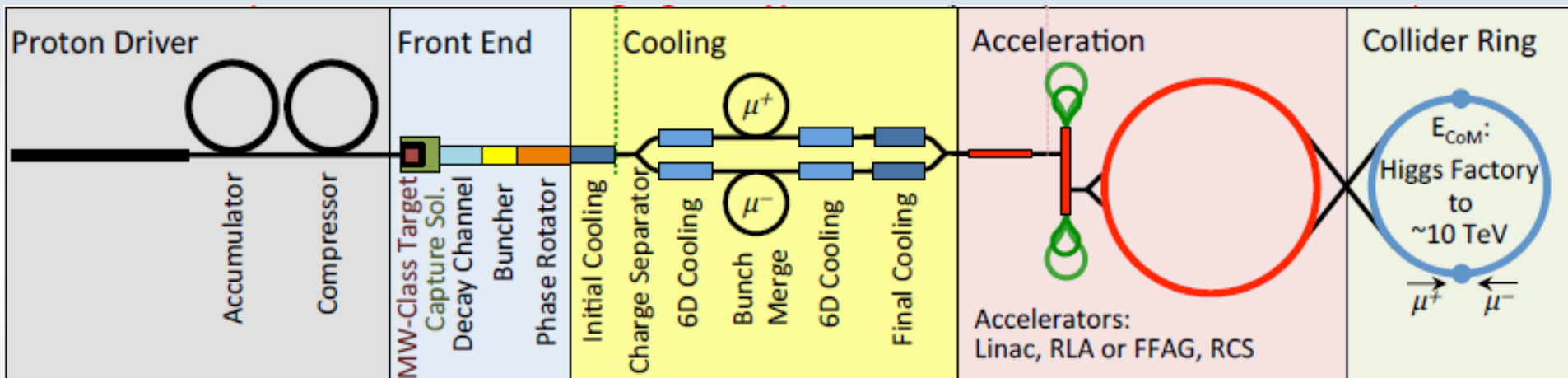


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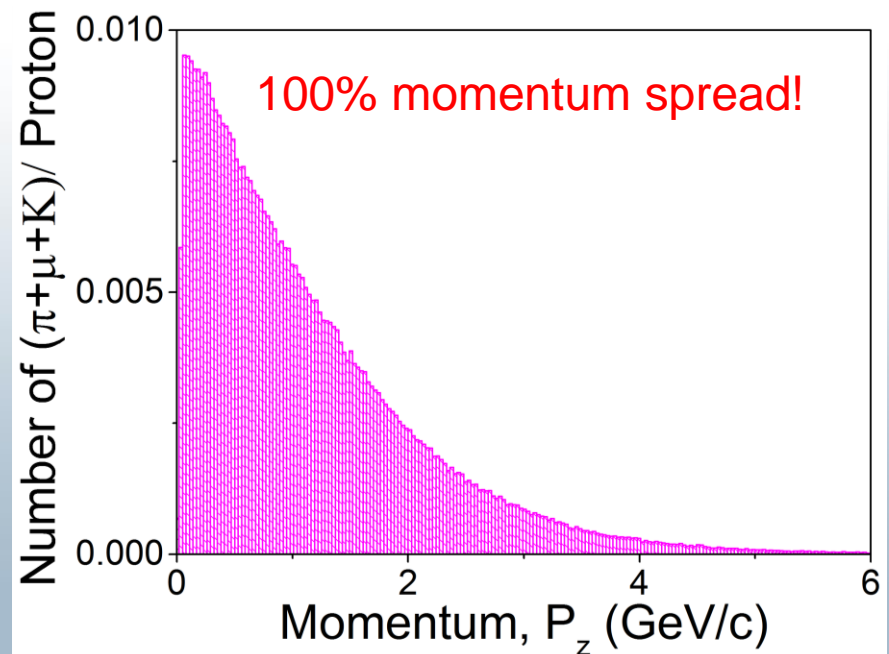
- The desired average luminosity of a MC is  $O(10^{34}) \text{ cm}^{-2}\text{s}^{-1}$

# Challenge #1

- Muons born as tertiary beams: Protons  $\rightarrow$  pions  $\rightarrow$  muons
- To achieve the desired luminosity it will require the production of  $10^{14}$  muons per second
- How to capture, manipulate and transport such intense muon beams?

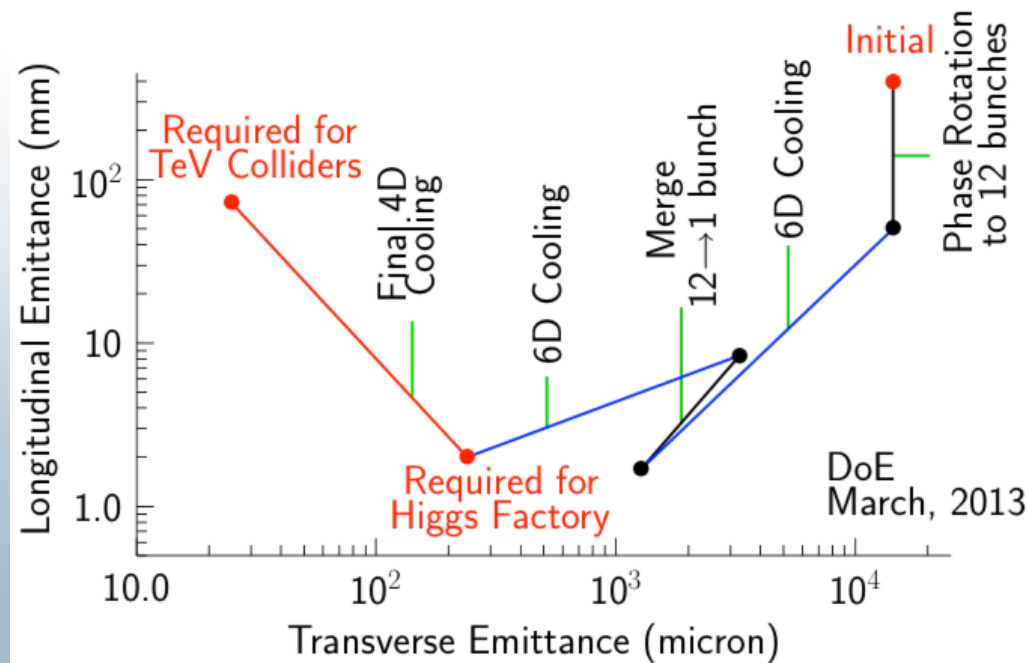
## Proton Driver:

Parameter	Value
Power	4 MW
Repetition rate	15 Hz
Proton Energy	8 GeV
Protons per pulse	$2.08 \times 10^{14}$
Rms pulse length	2 ns



# Challenge #2

- Initial beam occupies a very large phase-space area
- To obtain luminosities  $O(10^{34}) \text{ cm}^{-2}\text{s}^{-1}$  we need to reduce the initial phase-space by several orders of magnitude
- How to cool the muon beam fast?



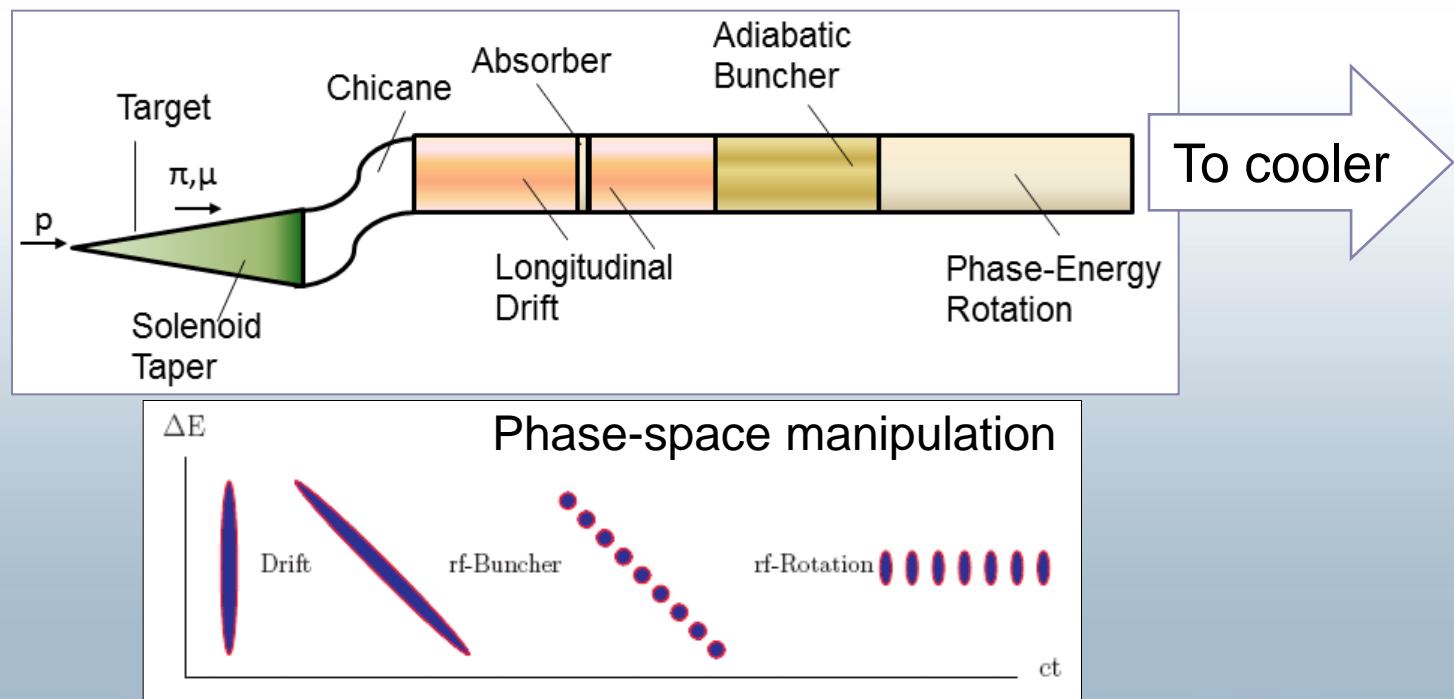
# Purpose of this work

- Present a efficient scheme to produce, manipulate and transport a muon beam
- Present a simple scheme to cool the 6D emittance of a muon beam up to 5 orders of magnitude
- Simulate the aforementioned concepts and present the results
- Discuss challenges and future work
- Summary



# Muon capture & transport scheme


- Capture muons that result from the pion decay that are produced by an intense proton beam impacting a target
- Manipulate the initial phase-space of these muons to make them well-suited to subsequent accelerator systems



# Relevant paper: Editor's highlights!

- Our review paper, that was published in Journal of Physics G received special attention!

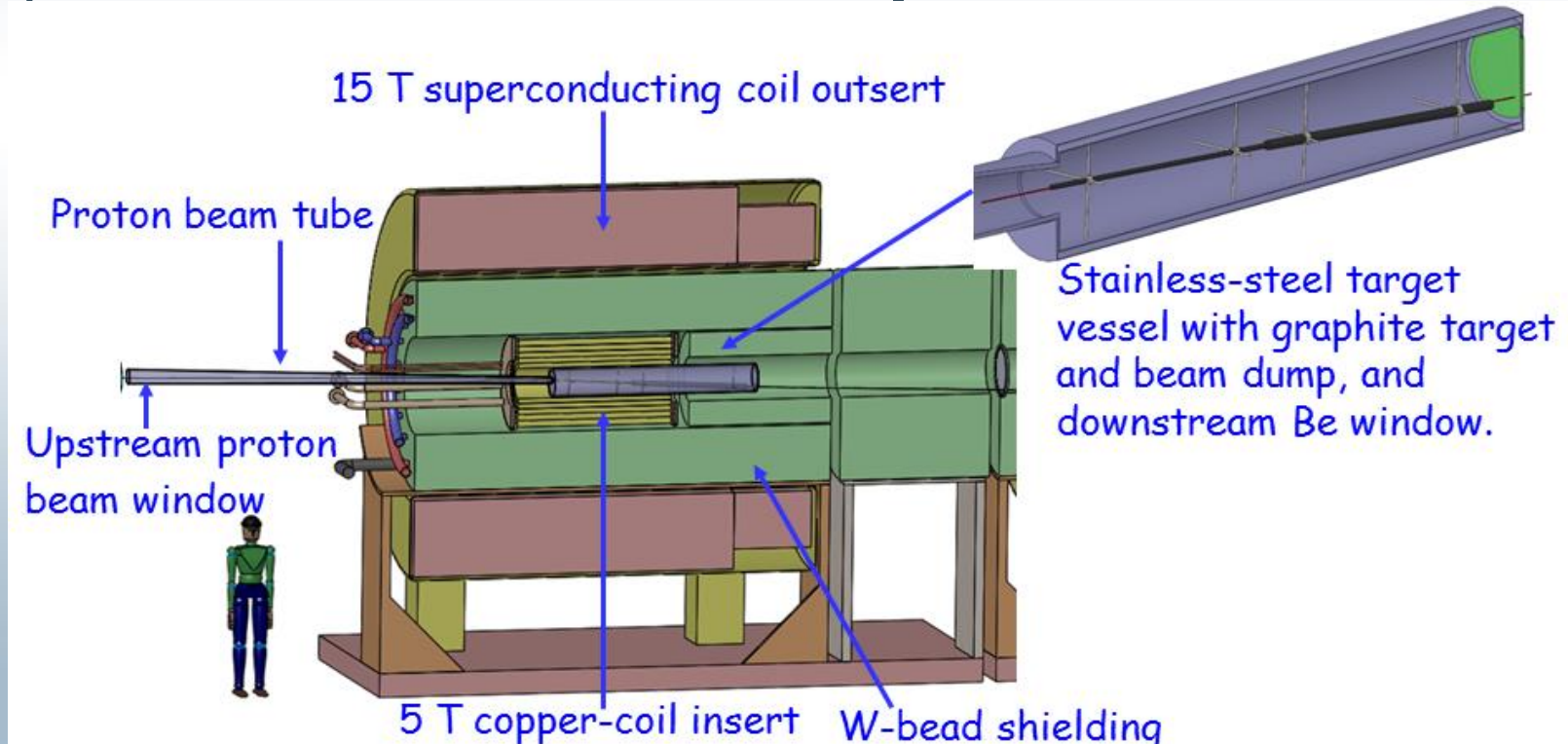
<b>IOP Publishing</b>	Journal of Physics G: Nuclear and Particle Physics
J. Phys. G: Nucl. Part. Phys. 41 (2014) 125002 (12pp)	doi:10.1088/0954-3899/41/12/125002
<b>Compact muon production and collection scheme for high-energy physics experiments</b>	
Diktys Stratakis <sup>1</sup> and David V Neuffer <sup>2</sup>	
<sup>1</sup> Brookhaven National Laboratory, Upton, NY 11973, USA	
<sup>2</sup> Fermi National Accelerator Laboratory, Batavia, IL 60510, USA	

<h2>Journal of Physics G</h2> <h3>Nuclear and Particle Physics</h3> <p><b>This is to certify that the article</b></p> <p><b>Compact muon production and collection scheme for high-energy physics experiments</b> <b>by Diktys Stratakis and David V Neuffer</b></p> <hr/> <p>has been selected by the editors of <i>Journal of Physics G: Nuclear and Particle Physics</i> for inclusion in the exclusive 'Highlights of 2014' collection. Papers are chosen on the basis of referee endorsement, novelty, scientific impact and broadness of appeal.</p> <div><p><b>Colin Adcock</b> Publisher <i>Journal of Physics G: Nuclear and Particle Physics</i> <a href="http://iopscience.org/jphysg">iopscience.org/jphysg</a></p><p><b>IOP Publishing</b></p></div>
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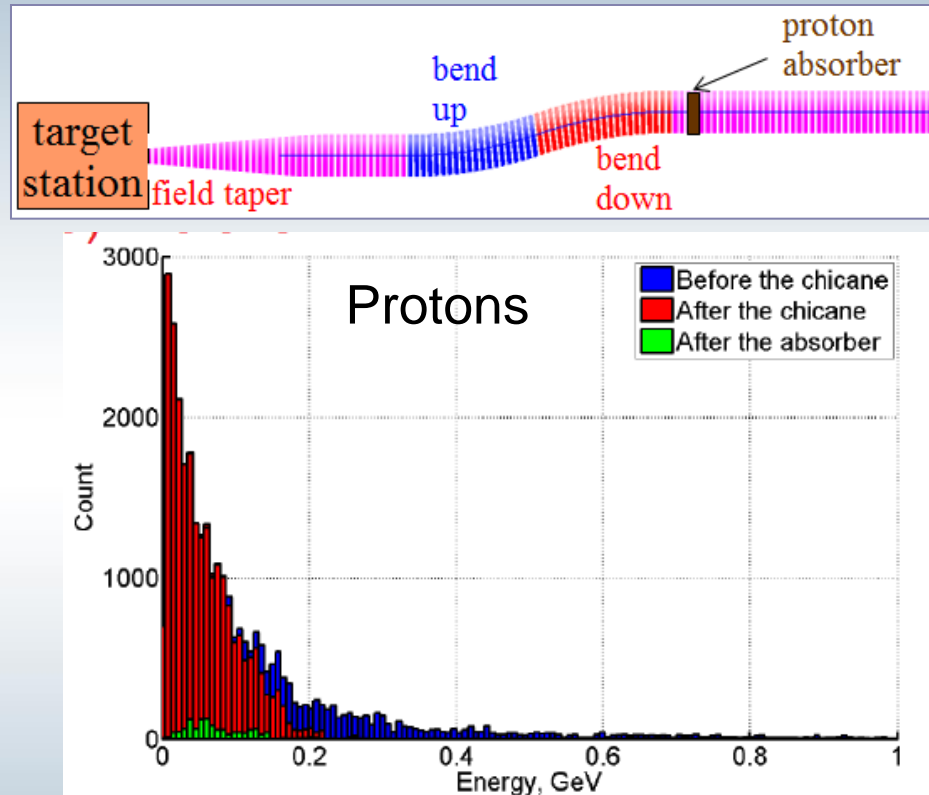
Download: <http://iopscience.iop.org/0954-3899/41/12/125002>

# Muon capture

- Target immersed in a 20 T solenoid that collects both  $\mu^+$   $\mu^-$
- Target and proton beam tilted with magnetic axis
- Optimized for maximum muon yield at  $40 < KE < 180$  MeV



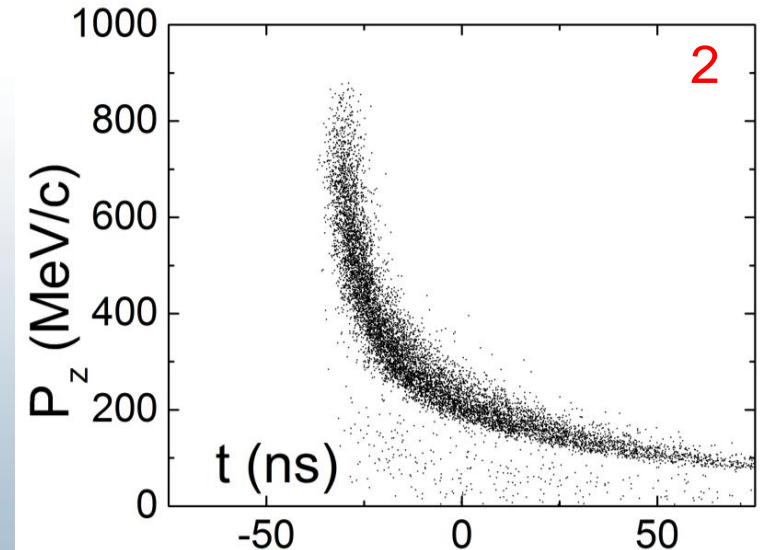
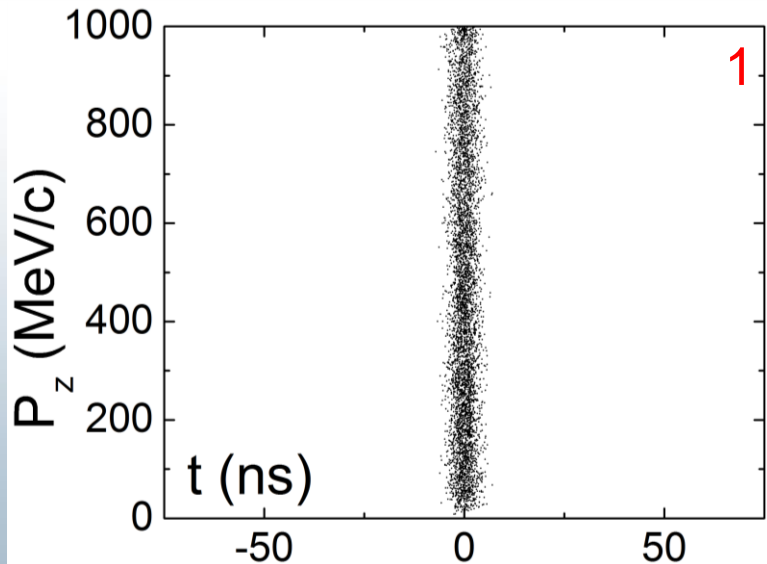
# Handling of secondary particles



- Bend solenoidal chicane induce dispersion to the beam so that high momentum particles scrape
- Proton absorber to remove low momentum protons

# Bunching & phase-rotation (1)

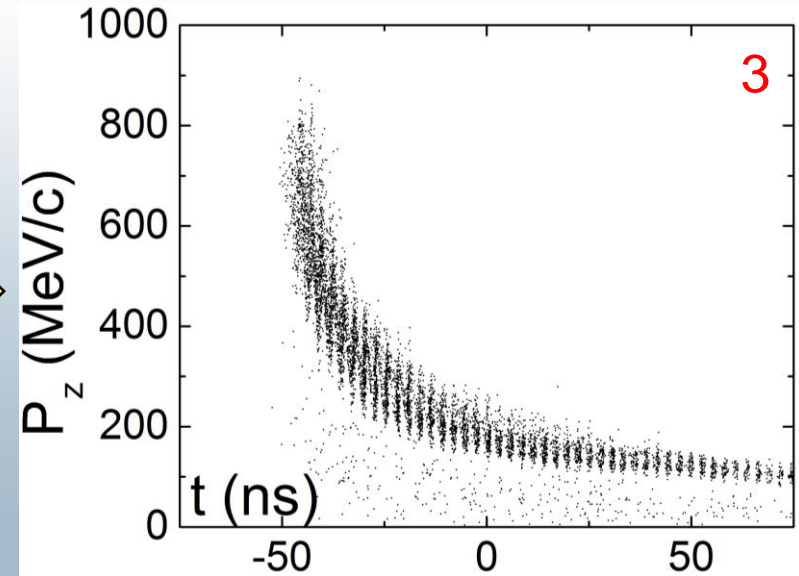
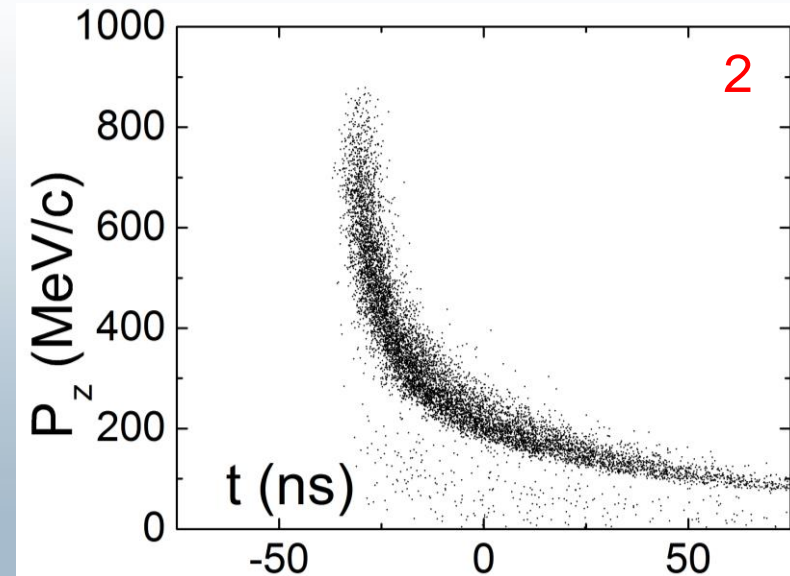
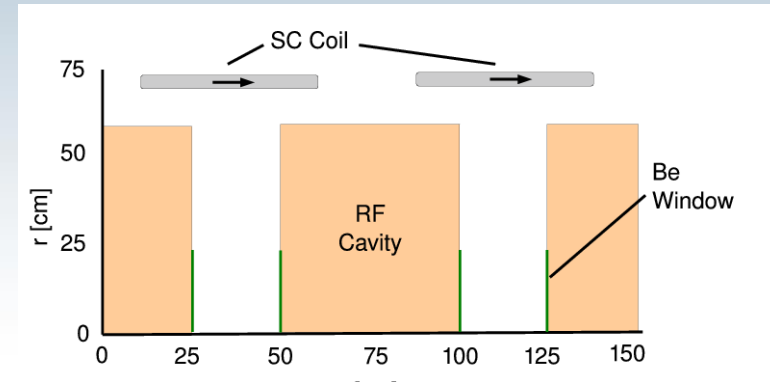
- After target, the beam is allowed to lengthen and develop a energy-time correlation [1→2]





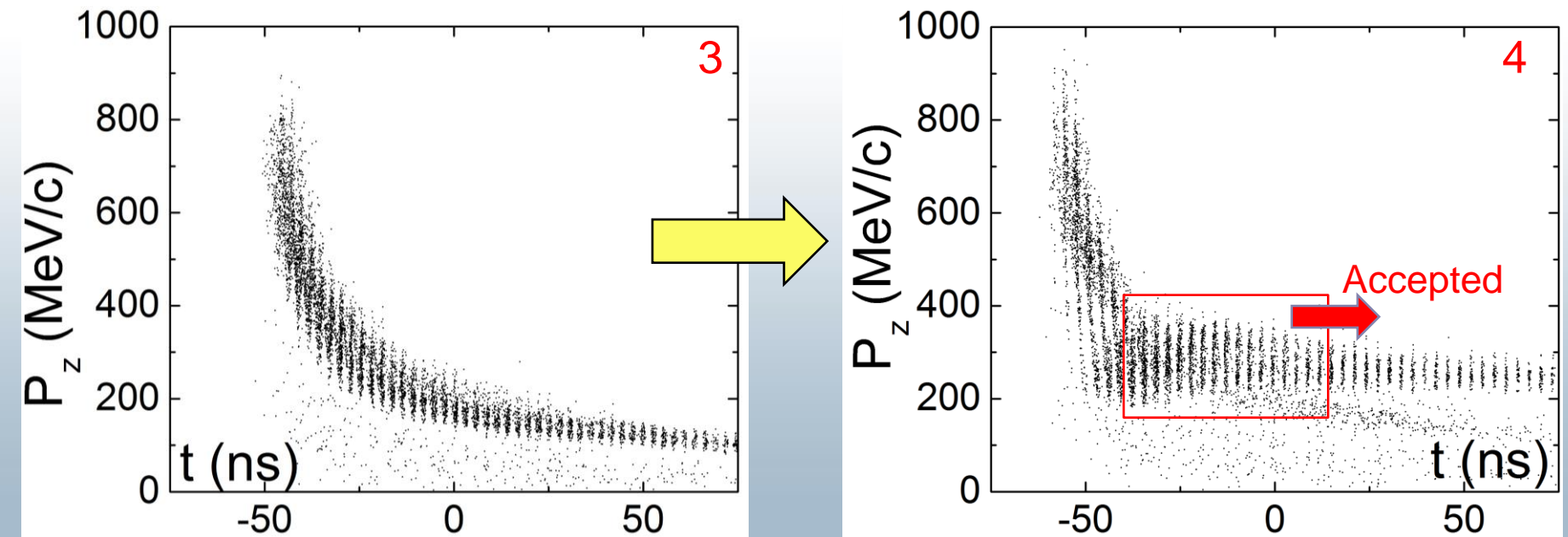
# Bunching & phase-rotation (2)

- Bunching with a set of rf cavities whose frequencies drop with distance (490-360 MHz) [2→3]



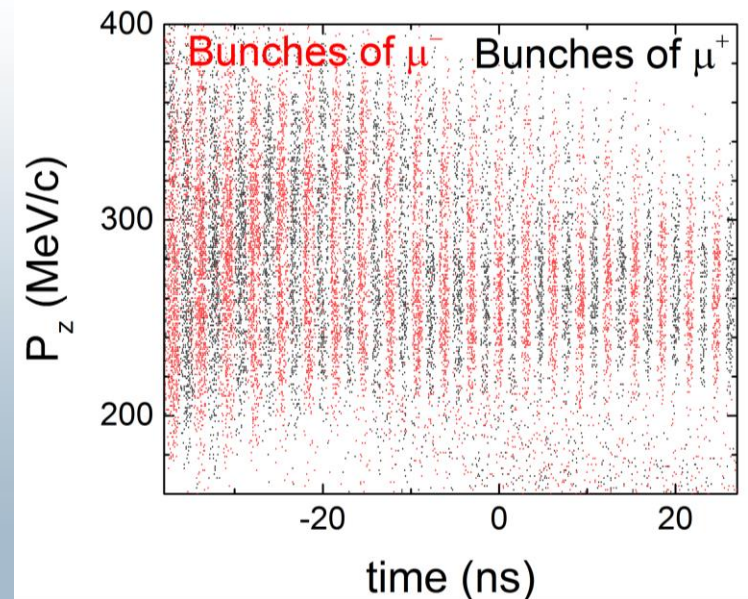
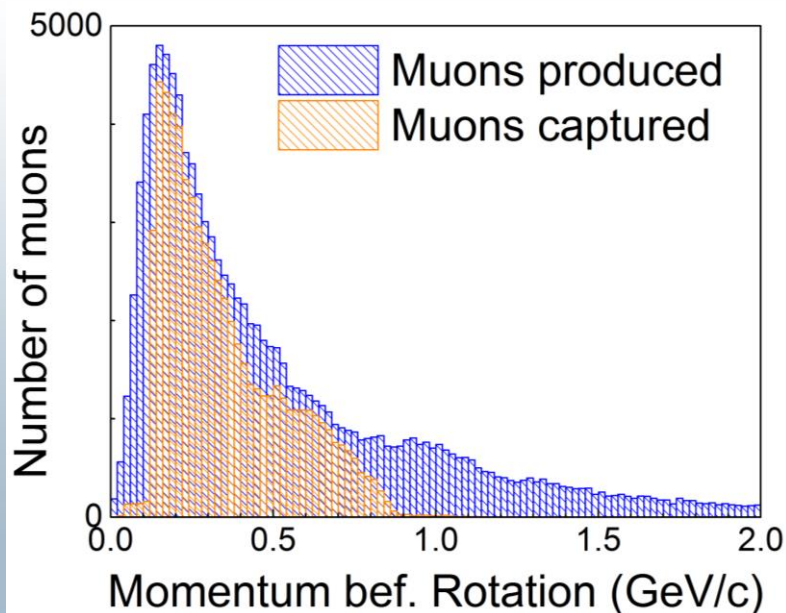
# Bunching & phase-rotation (3)

- After bunching, the beam is phase-rotated with a second set of rf cavities with decreasing frequencies (360-326 MHz) [3→4]

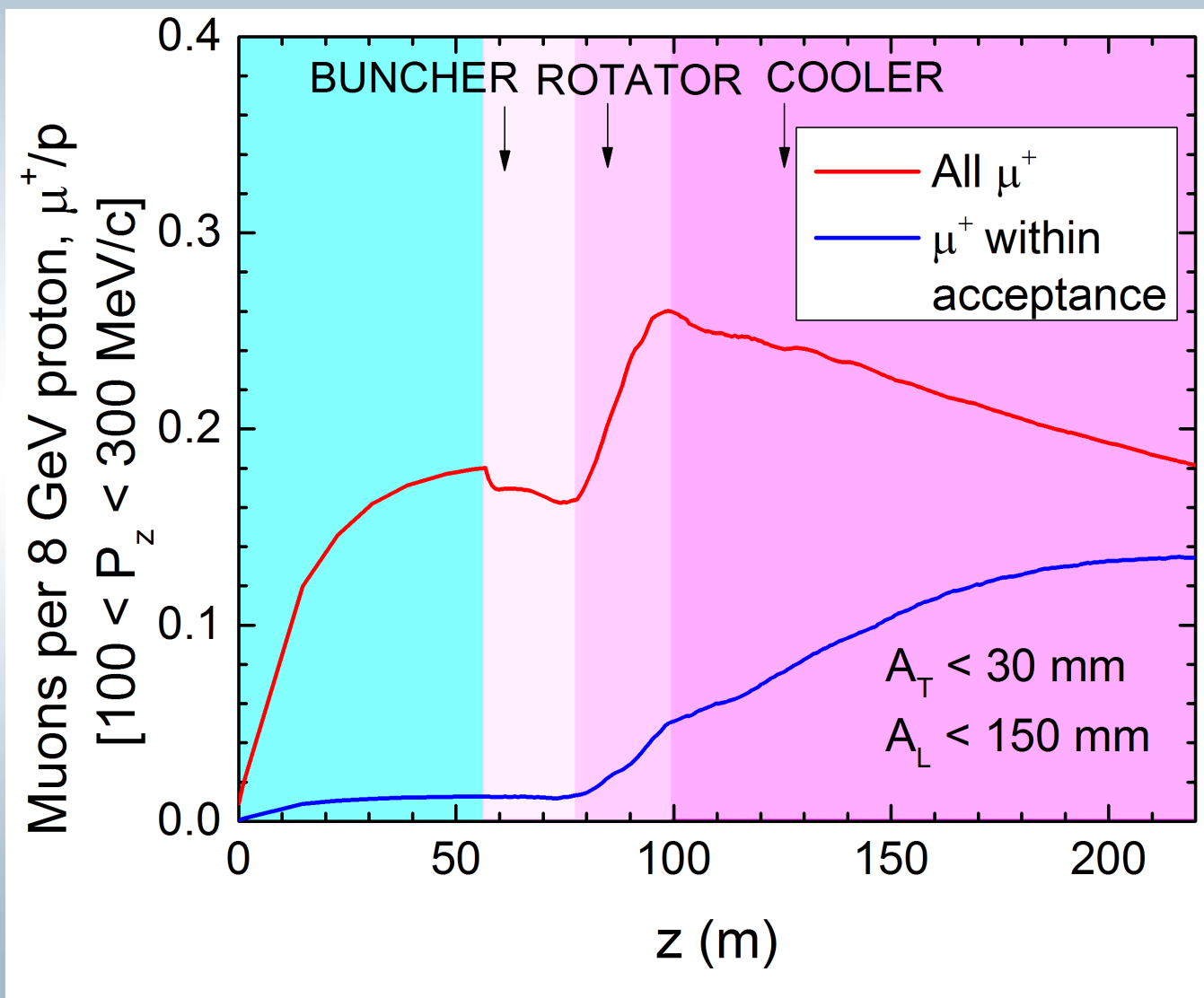


# Beam after phase-rotation

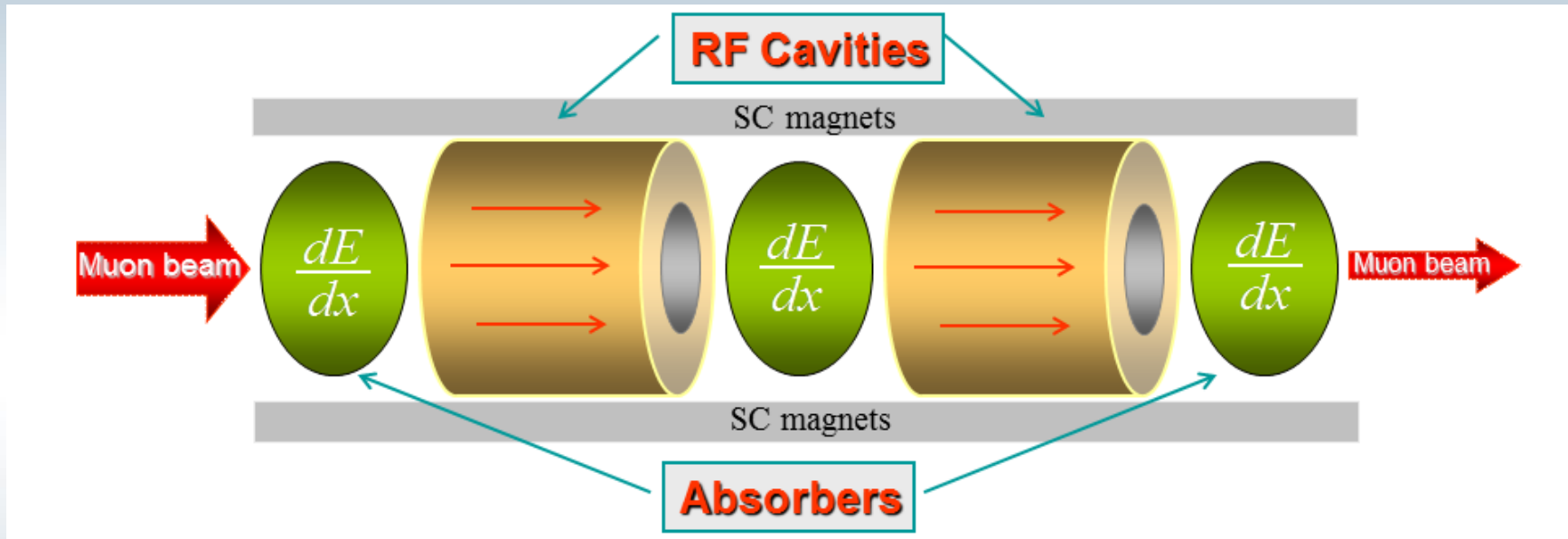
- Captured beam:
  - Both signs can be captured simultaneously
  - bunches spaced by 3.1 ns at 325 MHz
  - $\mu/p \approx 0.25$  per each sign per incident 8 GeV proton



# Muon production rate



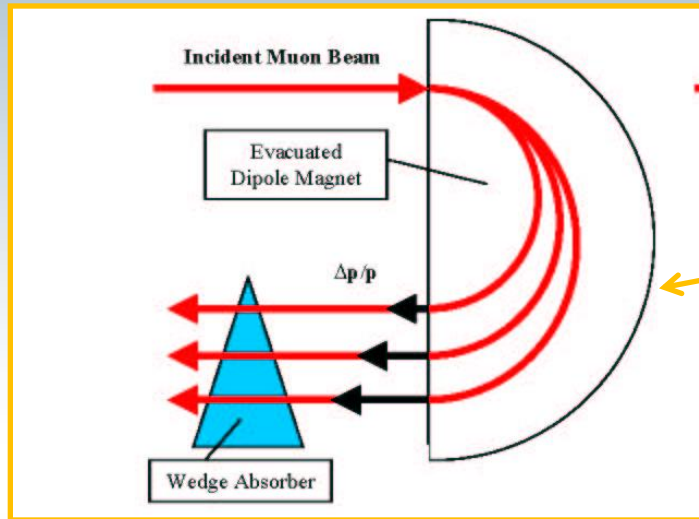
# Ionization cooling



- Energy loss through ionization in absorbers
- rf cavities to compensate for lost longitudinal energy
- Note: This process cools the beam transversely, only!

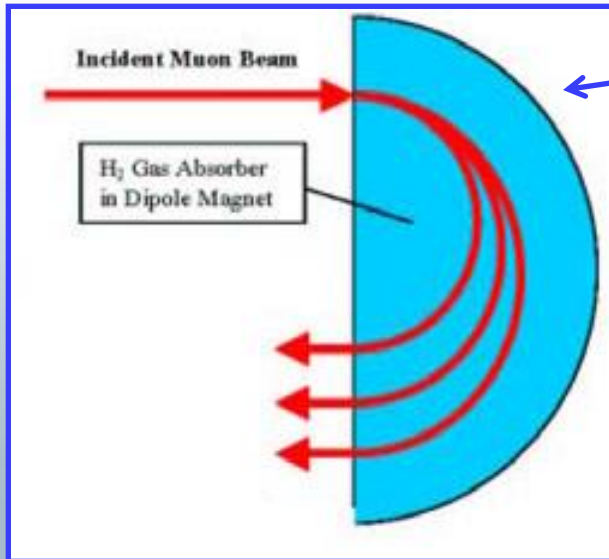


# Emittance exchange for 6D cooling



Concept 1: Generate dispersion and cool via emittance exchange in a wedge absorber

Concept 2: Energy loss dependence on path length in a continuous absorber



- Two concepts, same principle
- Dispersion is introduced to spatially separate muons of different momenta
- This study focuses on channels with discrete absorbers only!

# Ionization cooling basics

- In the absorber: Energy loss is causing **cooling**, BUT multiple scattering is causing **heating**.
- A balance between the two processes gives:

$$\varepsilon_T^{\text{eq}} = \left( \frac{dE}{ds} \right)^{-1} \frac{\beta_T (13.6 \text{ MeV})^2}{2\beta m_\mu c^2 L_R}$$

$L_R$ : Radiation length

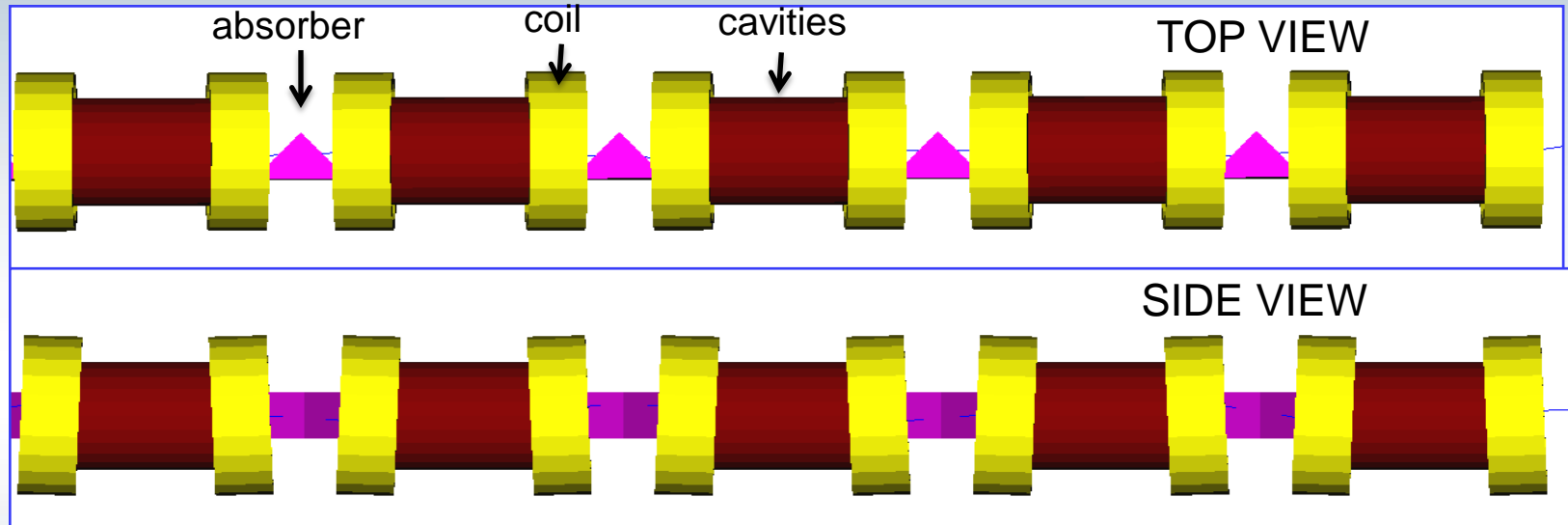
$E$ : Muon energy

$\beta_T$ : Transverse beta function

$\frac{dE}{ds}$ : Energy loss

- Emittance can be controlled by:
  - Material: Product of  $L_R$  and  $dE/ds$  should be large.
  - Magnet strength: Transverse beta function must be small. Thus, we progressively taper the magnetic field towards higher values

# Proposed cooling channel



- We considered a straight cooling scheme for a MC
- Idea originally proposed by Valeri Balbekov (Fermilab)
- Its simple geometry avoids several engineering challenges of previously considered schemes (rings or helix)

# More details

PHYSICAL REVIEW SPECIAL TOPICS - ACCELERATORS AND BEAMS 18, 031003 (2015)

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 **Editor's suggestion!**

## **Rectilinear six-dimensional ionization cooling channel for a muon collider: A theoretical and numerical study**

Diktys Stratakis and Robert B. Palmer

*Brookhaven National Laboratory, Upton, New York 11973, USA*

(Received 25 September 2014; published 6 March 2015)

A muon collider requires a reduction of the six-dimensional emittance of the captured muon beam by several orders of magnitude. In this study, we describe a novel rectilinear cooling scheme that should meet this requirement. First, we present the conceptual design of our proposed scheme wherein we detail its basic features. Then, we establish the theoretical framework to predict and evaluate the performance of ionization cooling channels and discuss its application to our specific case. Finally, we present the first end-to-end simulation of 6D cooling for a muon collider and show a notable reduction of the 6D emittance by 5 orders of magnitude. We find good agreement between simulation and theory.

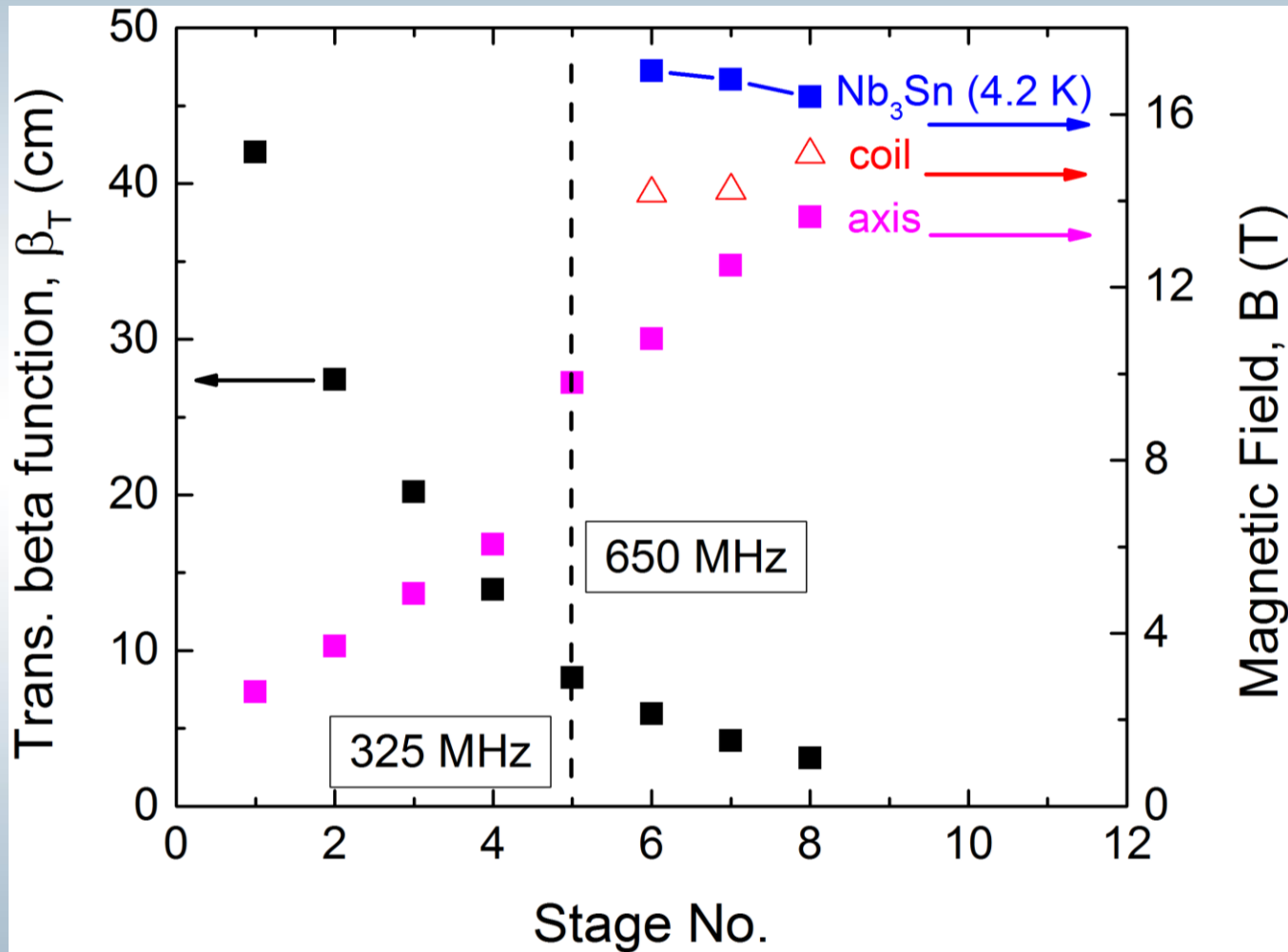
DOI: [10.1103/PhysRevSTAB.18.031003](https://doi.org/10.1103/PhysRevSTAB.18.031003)

PACS numbers: 29.20.Ej, 41.75.Lx

Download:

<http://journals.aps.org/prstab/abstract/10.1103/PhysRevSTAB.18.031003>

# Tapered lattice design: 8 stages

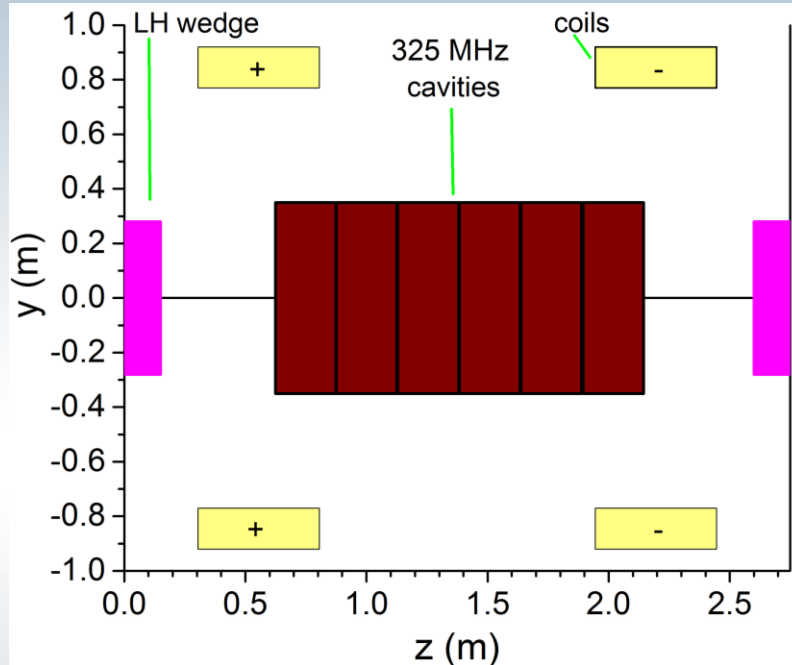


Magnet limits:

<https://nationalmaglab.org/magnet-development/applied-superconductivity-center/plots>

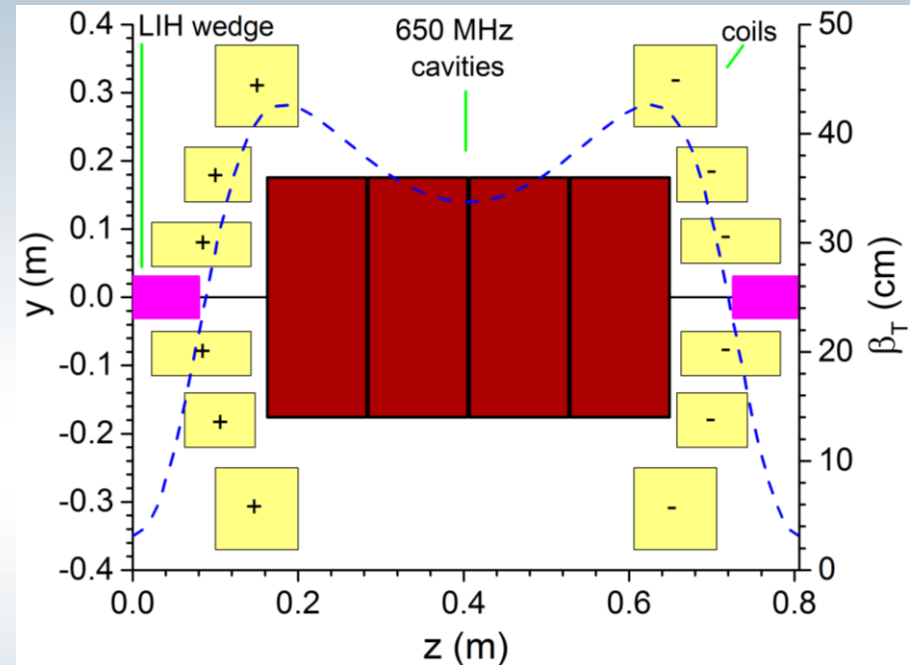


# Two extremes: First & last cooling stage



EARLY STAGE OF COOLING

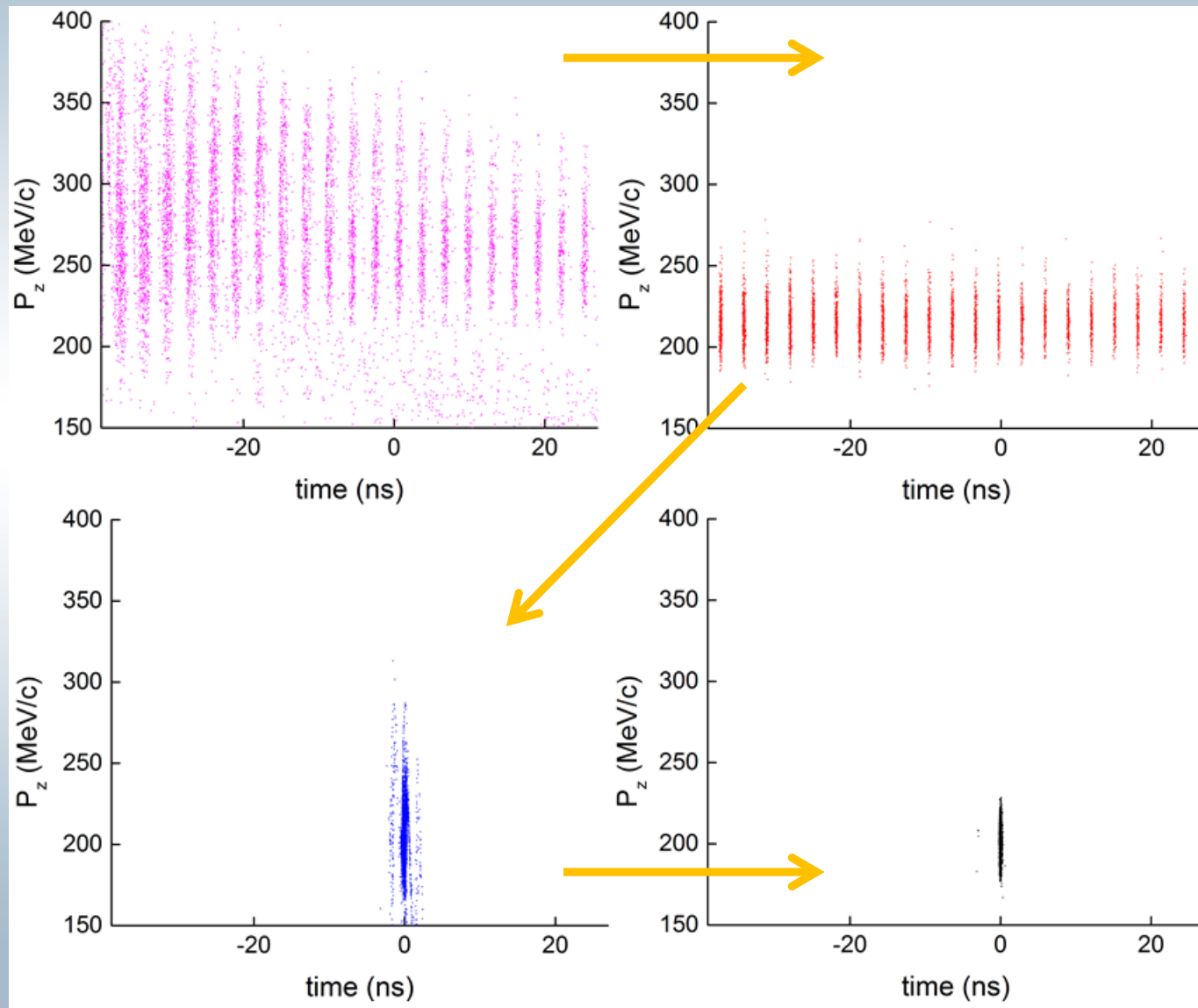
- 275 cm long
- Coils far
- 325 MHz
- Axial B ~ 3 T
- Beta ~ 40 cm



LATE STAGE OF COOLING

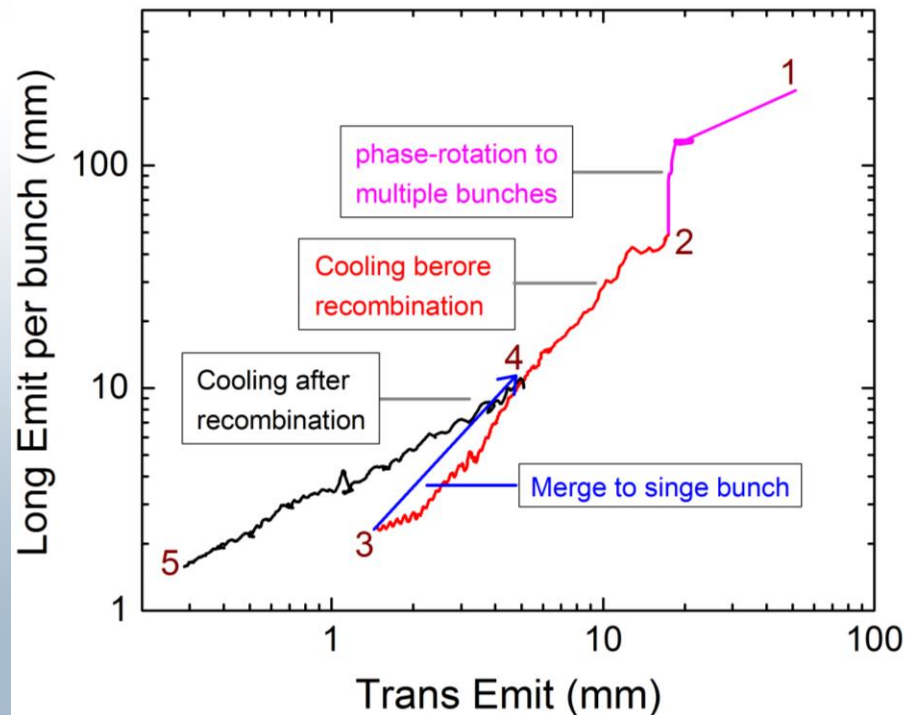
- 80 cm long
- Coils near axis
- 650 MHz
- Axial B ~ 12 T
- Beta ~ 3 cm

# Simulation results (1)



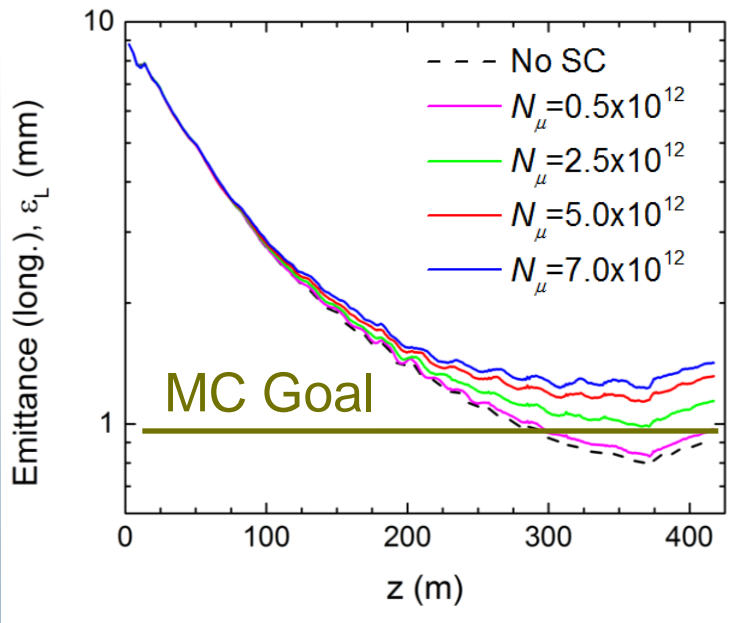
# Simulation results (2)

- End-to-end simulation starting from the target (point 1)
- Reduction of the 6D emittance by several orders of magnitude (point 5)
- Desired emittances for Higgs factory delivered!

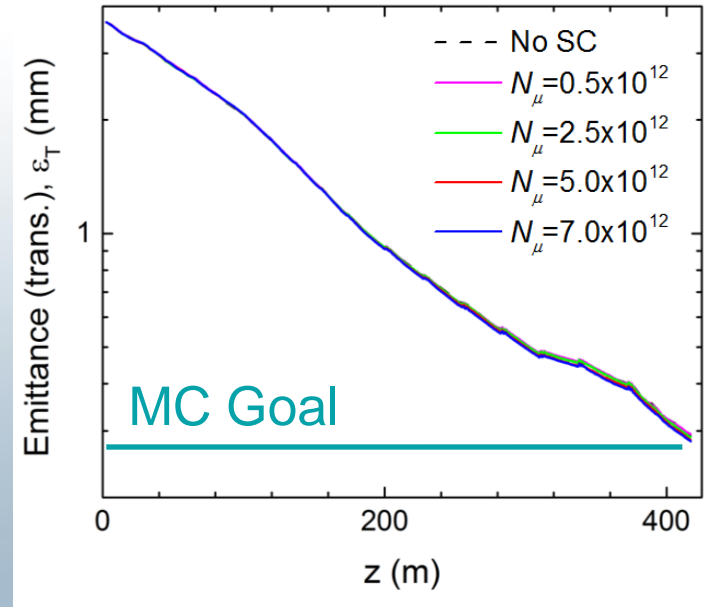


# Influence of space-charge (SC)

- At the end of cooling,  $5 \times 10^{12}$  muons are squeezed within a 2 cm rms bunch length. There is a concern for SC effect
- We examined the influence of SC fields on cooling
- SC causes particle loss & longitudinal emittance growth

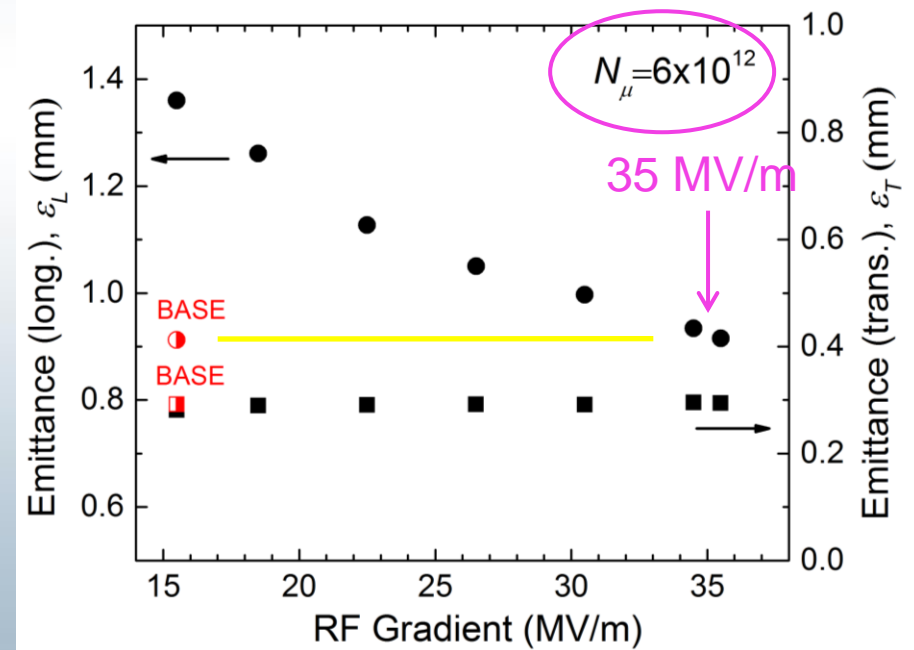
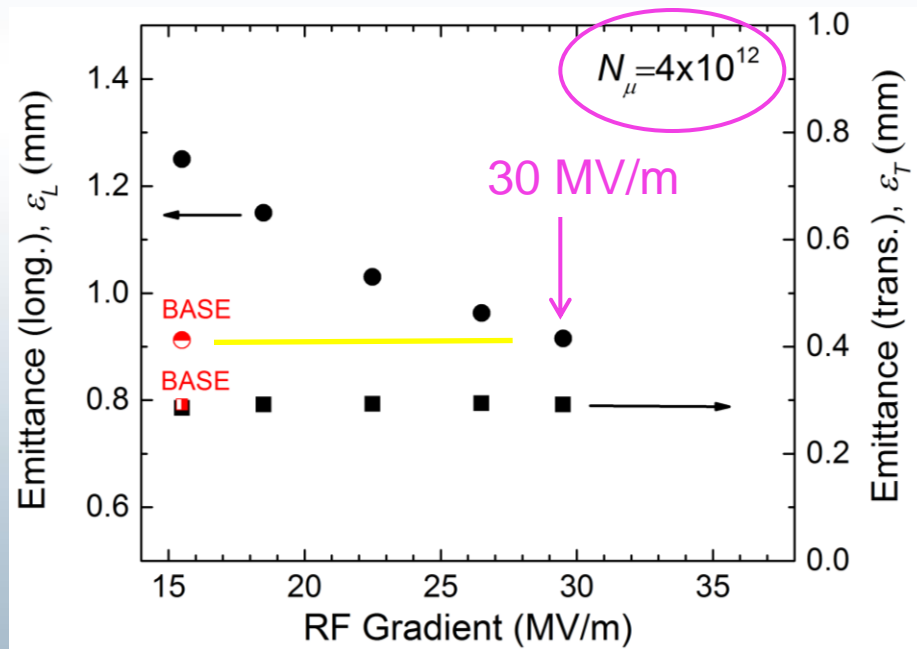


WARP  
Simulation



# Space-charge compensation (1)

- Increasing the rf gradient can compensate SC effect
- The needed compensation gradient is coupled to the beam intensity

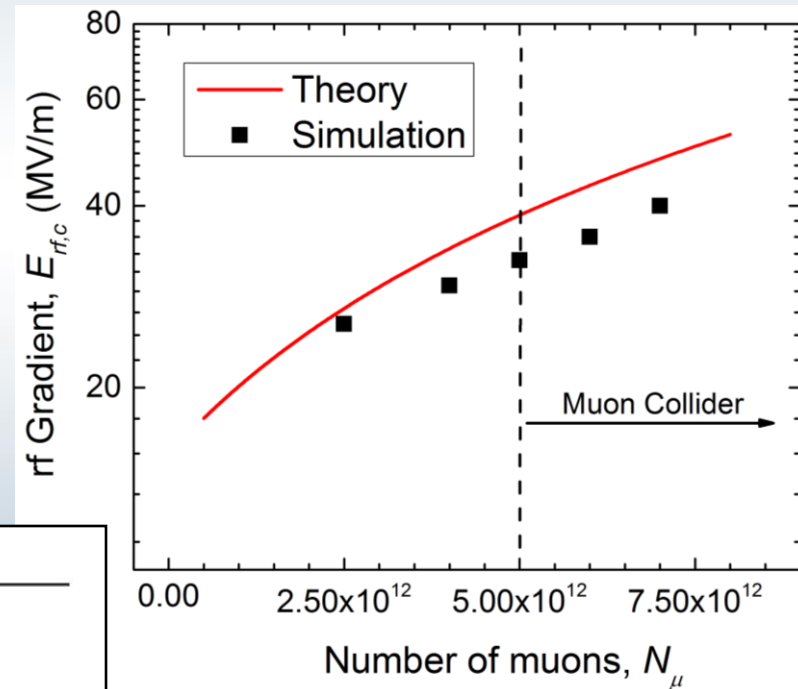




# Space-charge compensation (2)

- For a MC to obtain a  $\varepsilon_L < 1.0$  mm the rf gradient of a 805 MHz cavity needs to surpass 32.5 MV/m
- Can be a problem (next slide)
- Required compensation gradient from theory:

$$E_{rf,c} = \frac{eN_0 g_0 c}{4\pi\epsilon_0 \sqrt{2\pi\gamma^2} \sigma_z^3 (2\pi f n \cos\phi)^3}$$



PHYSICAL REVIEW SPECIAL TOPICS - ACCELERATORS AND BEAMS **18**, 044201 (2015)

 **Editor's suggestion**

**Influence of space-charge fields on the cooling process of muon beams**

Diktys Stratakis and Robert B. Palmer

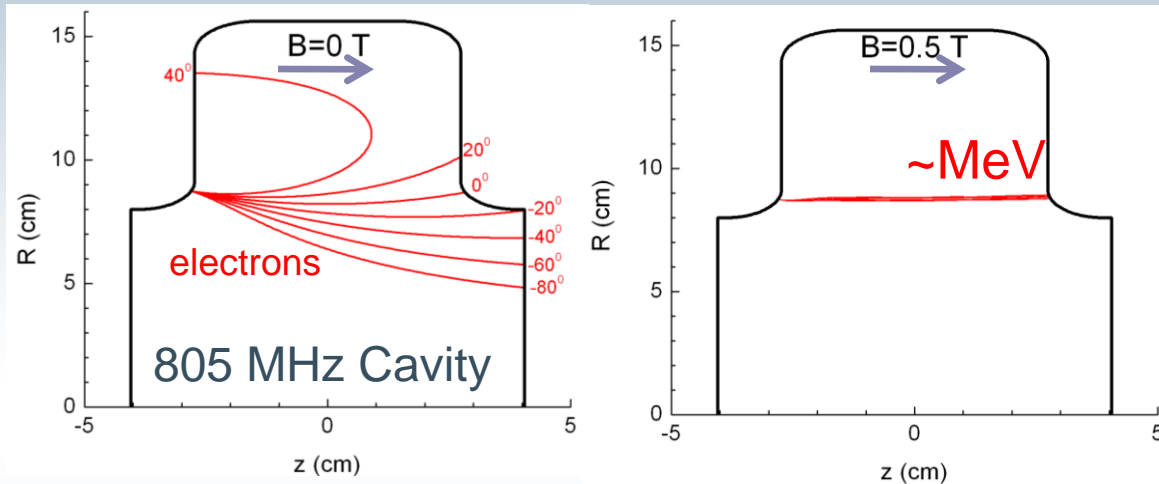
Brookhaven National Laboratory, Upton, New York 11973, USA

David P. Grote

Lawrence Livermore National Laboratory, Livermore, California 94550, USA

(Received 15 November 2014; published 7 April 2015)

# A challenge: rf operation in B-fields



Damage on a 805 MHz rf cavity immersed in a multi-T magnetic field.

- Numerical simulations predict that the copper surfaces of a rf cavity may be damaged when  $B > 1\text{ T}$

Contents lists available at ScienceDirect

**Nuclear Instruments and Methods in Physics Research A**

journal homepage: [www.elsevier.com/locate/nima](http://www.elsevier.com/locate/nima)

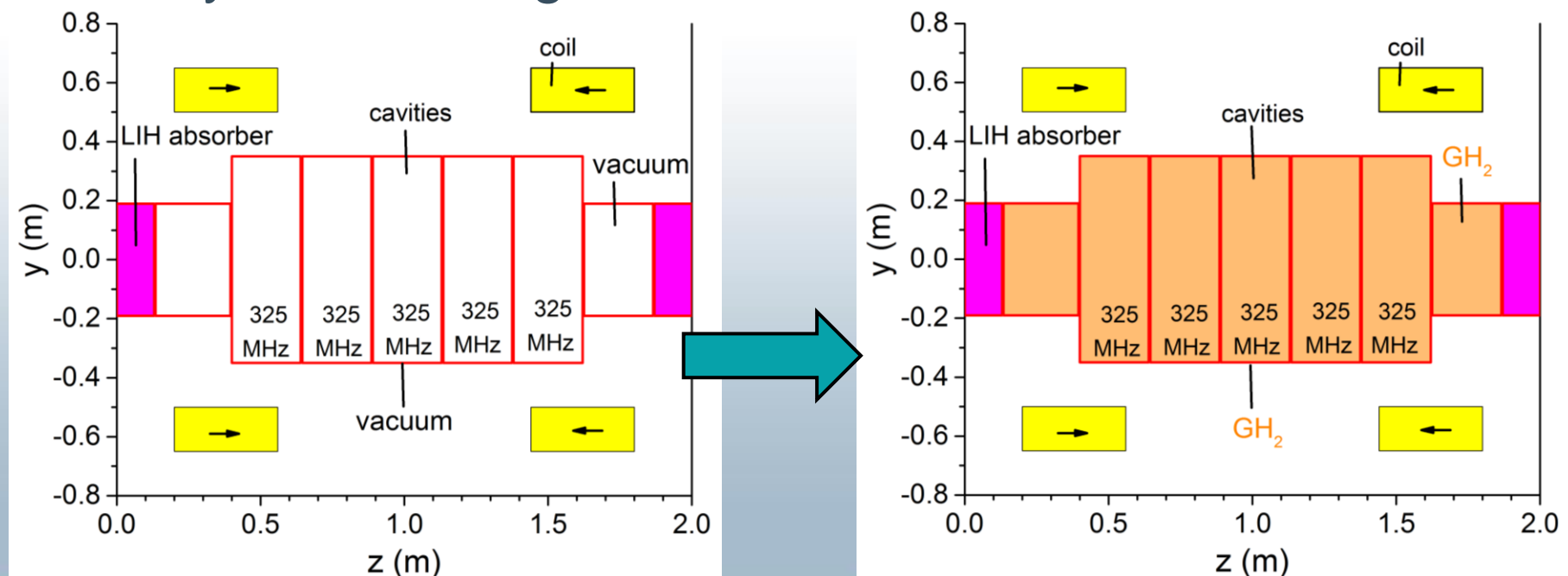
ELSEVIER

**Effects of external magnetic fields on the operation of high-gradient accelerating structures**

Dikty Stratakis\*, Juan C. Gallardo, Robert B. Palmer

# Hybrid solution

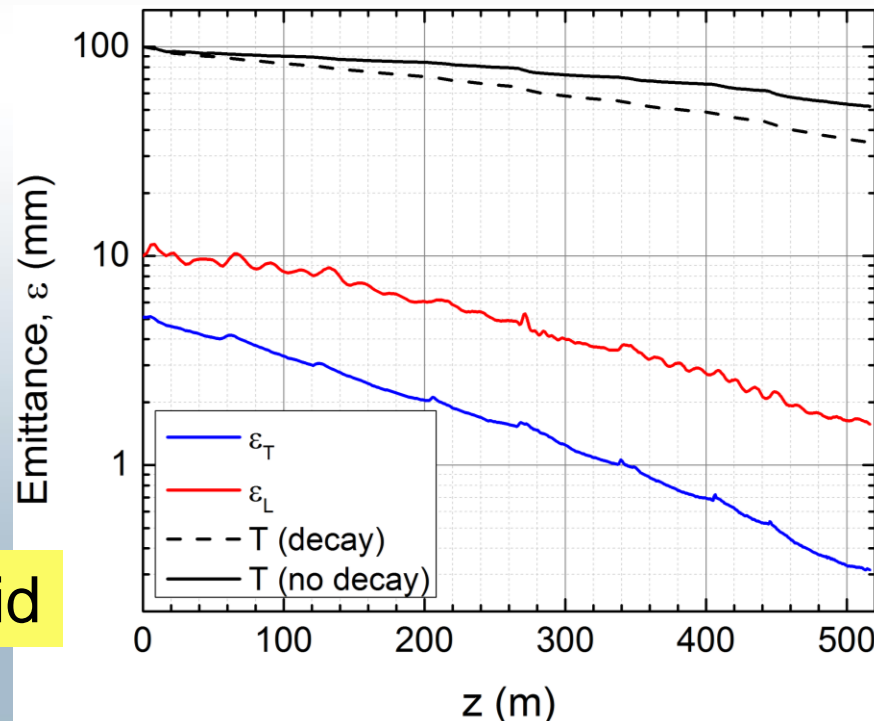
- The gradient of a gas filled cavity showed no magnetic field dependence in a solenoidal field up to 3 T.
- Key Idea: Utilize gas filled cavities in a rectilinear channel. Majority of cooling in LiH and use gas only to protect rf cavity from the high-field.



# Lattice performance

- Essentially, the same performance as an equivalent channel with vacuum cavities
- BUT there remains considerable work to do before a hybrid channel can be considered a validated cooling channel option.

Hybrid



# Future work – Open problems

- Energy deposition studies
  - Study on the target, chicane and rest of the channel
- Improve design of muon capture channel
  - Increase performance
- Reduce length of the cooling channel
  - Existing channel for a MC is 900 m ...
- Physics problems
  - Wakefields, absorbers, plasma loading
- Engineering problems
  - Magnets, cavities in magnetic fields, ...

# Summary

- Presented a scheme to collect & transport intense muon beams.
- Simulations show that it produces  $0.25 \mu/p$  with a relatively good degree of efficiency ( $\sim 60\%$ )
- Presented a simple scheme for ionization cooling
- Simulations predict that is capable to reduce the 6D emittance by at least five orders of magnitude thus satisfying the needs of a Higgs factory.
- The influence of space-charge fields on the cooling process was thoroughly examined
- A hybrid solution with gas filled cavities was presented



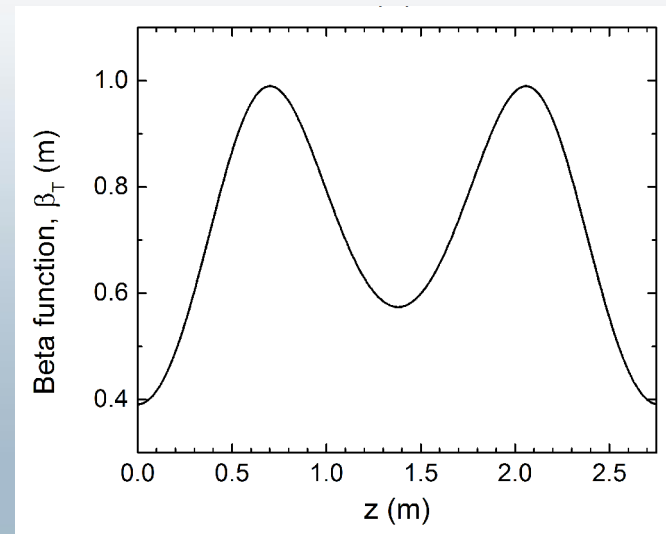
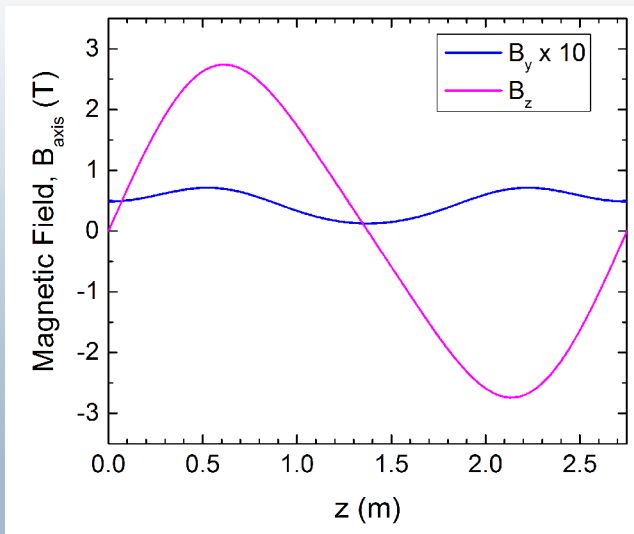
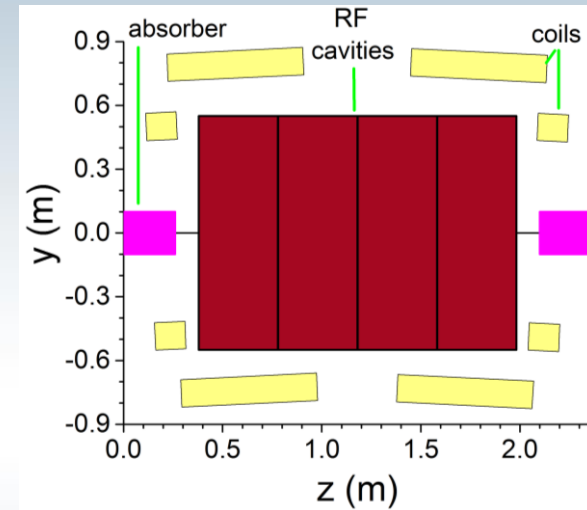
# Acknowledgement



- Special thanks to all members of the Muon Accelerator Program community

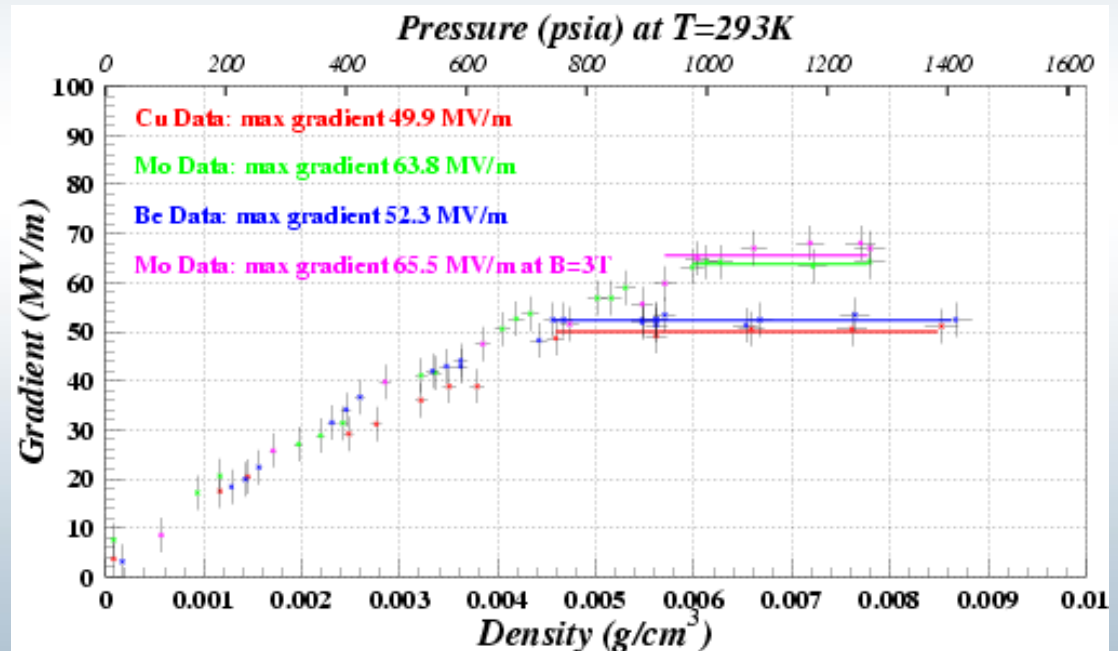
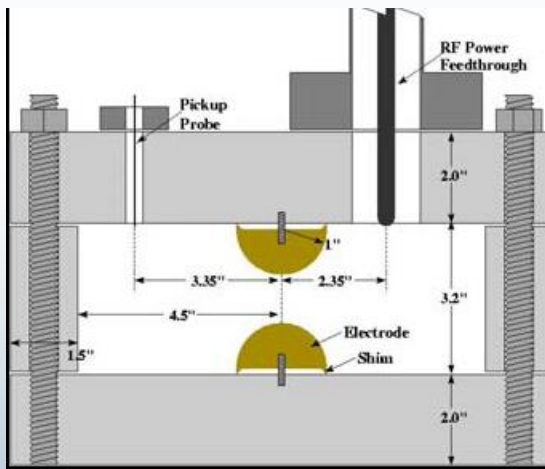
# Cooling channel: How it works

- Coils tilted to create a  $B_y$  component
- This leads to dispersion  $\rightarrow$  High momentum particles pass through more material  $\rightarrow$  6D cooling
- Absorber is placed at the point where  $\beta_T$  is minimum



# Back-up : Gas-filled cavities

- The gradient of a gas filled cavity showed no magnetic field dependence in a solenoidal field up to 3 T.

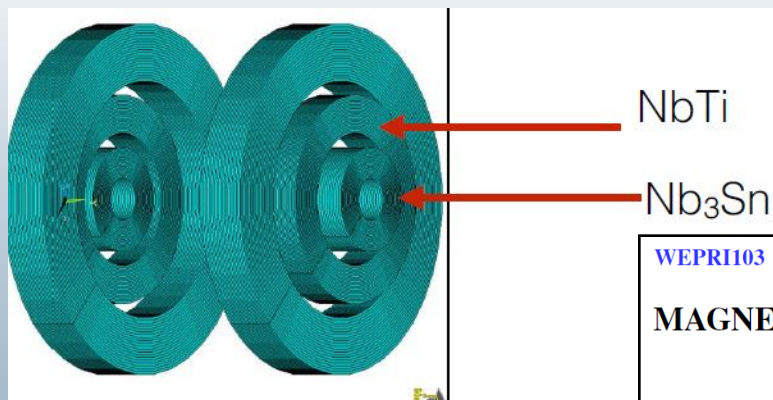
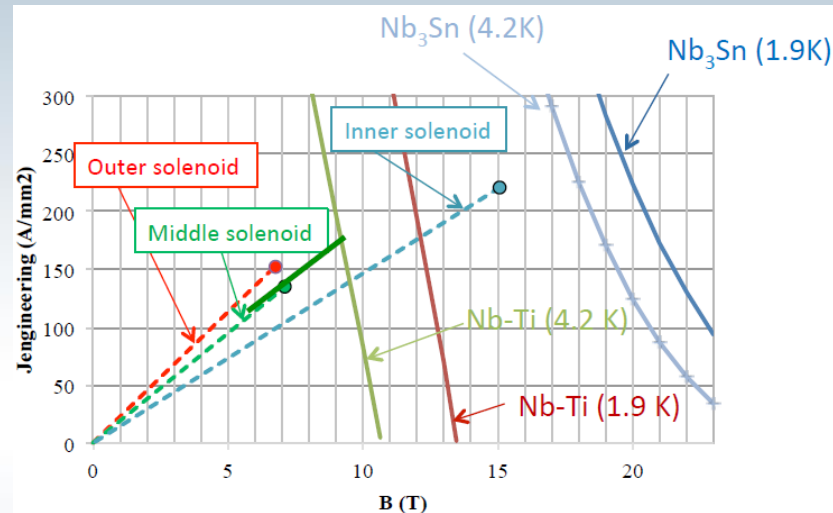
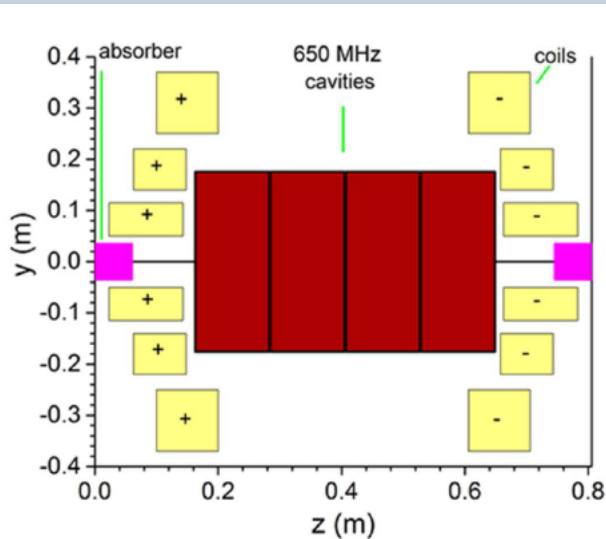


P. Hanlet et al., EPAC 2006, p. 1364 (2006)  
M. Chung et al., PRL 111, 184802 (2013)

# Back up: Muon Collider Parameters

Muon Collider Parameters								
		Higgs Factory		Top Threshold Options		Multi-TeV Baselines		
Parameter	Units	Startup Operation	Production Operation	High Resolution	High Luminosity			Accounts for Site Radiation Mitigation
CoM Energy	TeV	0.126	0.126	0.35	0.35	1.5	3.0	6.0
Avg. Luminosity	$10^{34} \text{cm}^{-2} \text{s}^{-1}$	0.0017	0.008	0.07	0.6	1.25	4.4	12
Beam Energy Spread	%	0.003	0.004	0.01	0.1	0.1	0.1	0.1
Higgs* or Top* Production/ $10^7 \text{sec}$		3,500*	13,500*	7,000*	60,000*	37,500*	200,000*	820,000*
Circumference	km	0.3	0.3	0.7	0.7	2.5	4.5	6
No. of IPs		1	1	1	1	2	2	2
Repetition Rate	Hz	30	15	15	15	15	12	6
$\beta^*$	cm	3.3	1.7	1.5	0.5	1 (0.5-2)	0.5 (0.3-3)	0.25
No. muons/bunch	$10^{12}$	2	4	4	3	2	2	2
No. bunches/beam		1	1	1	1	1	1	1
Norm. Trans. Emittance, $\epsilon_{\text{TN}}$	$\pi \text{ mm-rad}$	0.4	0.2	0.2	0.05	0.025	0.025	0.025
Norm. Long. Emittance, $\epsilon_{\text{LN}}$	$\pi \text{ mm-rad}$	1	1.5	1.5	10	70	70	70
Bunch Length, $\sigma_s$	cm	5.6	6.3	0.9	0.5	1	0.5	0.2
Proton Driver Power	MW	4 <sup>#</sup>	4	4	4	4	4	1.6

# Back up: Magnet feasibility (last stage)



	% of the load line at operational current		
	Inner solenoid	Middle solenoid	Outer solenoid
Nb-Ti @ 4.2 K	-	76%	74%
Nb-Ti @ 1.9 K	-	59%	58%
Nb3Sn @ 4.2 K	88%	-	-
Nb3Sn @ 1.9 K	81%	-	-

WEPRI103

Proceedings of IPAC2014, Dresden, Germany

## MAGNET DESIGN FOR A SIX-DIMENSIONAL RECTILINEAR COOLING CHANNEL - FEASIBILITY STUDY\*

H. Witte<sup>†</sup>, D. Stratakis, J. S. Berg, R. B. Palmer, Brookhaven National Laboratory, Upton, NY, USA  
F. Borgnolutti, Lawrence Berkeley National Laboratory, Berkeley, CA, USA



# Back up: Buncher & rotator parameters

Match to 325 MHz*	Len. (m)	No. of RF	f (MHz)	RF grad. (MV/m)	B axis (T)
Buncher	21	28	490.0 to 365.0	0.0 to 15.0	2.0
Rotator	24	32	364.0 to 326.0	20.0	2.0
Total	45	60			

\*Currently under study